

PROTOTYPE STUDY OF THE STRAW  
TUBE PROPORTIONAL CHAMBER

C. Lu, K.T. McDonald and D. Secret

*Joseph Henry Laboratories, Princeton University, Princeton, NJ 08544*

**Abstract**

In our "Proposal to the SSC Laboratory for Research and Development of a Straw-Tube Tracking Subsystem" we have raised several issues important for operating a large straw-tube tracking system in the SSC environment. This paper reports on prototype studies of the validity of various models of the gas-gain mechanism, of temperature dependence of gas gain, and of electrostatic stability of a long straw tube and some related problems.

**1. Gas-gain study**

In designing a gas wire chamber, the gas gain always is one of the most important and most basic considerations. Many experimental studies have been carried out to determine the gas gain of various counters under differing gas conditions, and several gas-gain formulae to fit the experimental data have been proposed.<sup>1-7</sup> It will be useful to identify the theoretical formula which best fits our straw-tube data.

A prototype module of straw tubes has been used for this study. It consists of seven short straw-tube counters, each 7 cm in length and 0.7 cm in diameter. The straw tube itself is made of a two-ply laminate of an inner polycarbonate film about 14  $\mu\text{m}$  thick surrounded by a layer of 12.5- $\mu\text{m}$  Mylar. The polycarbonate film is aluminized on its inner surface to about 1000  $\text{\AA}$  thickness. The tubes and end plugs were obtained from Ohio State U.<sup>8</sup> The seven tubes have five different anode wire sizes: 0.0203, 0.0254, 0.051, 0.076, and 0.127 mm diameter.

Two kinds of gas mixtures, P-10 [= Ar/CH<sub>4</sub> (90/10)] and Ar/C<sub>2</sub>H<sub>6</sub> (50/50), have been tested with this prototype thus far. We used an Fe<sup>55</sup> source and measured the charge out of the test chamber with an Ortec model 142PC preamplifier, followed by an Ortec model 570 spectroscopy amplifier, whose output was digitized by an Ortec model 916 multichannel analyzer. A calibration of the charge out of the chamber per count in the 916 analyzer was obtained with an Ortec model 419 precision pulser (by charging a 2 pf capacitor). The primary ionization caused by the Fe<sup>55</sup> is taken to be 224 electrons in P-10 and 232 electrons in Ar/Ethane. This is based on an average energy loss per ion pair created of 26.3 eV in P-10 and 25.4 eV in Ar/Ethane,<sup>9</sup> noting that the x-ray energy is 5.9 keV.

The data on gas gain *vs.* high voltage are shown in Fig. 1. For gas gains larger than  $2.5 \times 10^4$ , the signal charge due to the 5.9-keV x-rays will exceed 1

pC and the chamber will no longer be in the proportional mode. Therefore we have restricted our studies to gains below this value.

Among various gas-gain formulae, we used three to fit our experimental data, namely those of Diethorn,<sup>2</sup> Aoyama,<sup>6</sup> and Kowalski.<sup>7</sup>

Diethorn's formula is

$$\frac{\ln G}{V/\ln(R_c/R_a)} = \frac{\ln 2}{\Delta V} \left( \frac{\ln V}{PR_a \ln(R_c/R_a)} - \ln K \right). \quad (1)$$

Here  $\Delta V$  corresponds to the potential difference through which an electron moves between successive ionizing collisions, and  $K$  is the minimum value of  $E/P$  below which multiplication cannot occur. Throughout this paper,  $G$  is the gas gain,  $V$  is the voltage applied to the tube,  $E$  is the (position dependent) electric field strength,  $P$  is the pressure,  $R_a$  is the radius of the anode wire, and  $R_c$  is the radius of the cathode surface of the straw tube.

Aoyama's formula is

$$\frac{\ln G}{V/\ln(R_c/R_a)} = \exp \left\{ -A \left( \frac{V}{NR_a \ln(R_c/R_a)} \right)^{m-1} - \ln[(1-m)V_I] \right\}, \quad (2)$$

where  $V_I$  is the effective ionization potential, and  $A$  and  $m$  are constants characteristic of the gas.

**Table 1.** Variances and parameters of the fitting.

Gas mix	Fit type	Variance	Fitted parameter
P-10	Diethorn	$1.079 \times 10^{-6}$	$\Delta V = 33.35$ eV; $K = 3.411 \times 10^4$ V/cm·atm
	Aoyama	$0.898 \times 10^{-6}$	$A = 0.9625 \times 10^{-7}$ ; $m = 0.4954$ , $V_i = 14.4$ V
	Kowalski	$0.864 \times 10^{-6}$	$A_1 = 0.3848 \times 10^{-2}$ (m·Pa) $^{d-1}$ V $^{-d}$ ; $d = 1.359$ , $B_1 = -0.03384$ /V
Ar/Ethane (50/50)	Diethorn	$2.014 \times 10^{-7}$	$\Delta V = 31.58$ eV; $K = 4.84 \times 10^4$ V/cm·atm
	Aoyama	$1.141 \times 10^{-7}$	$A = 0.1141 \times 10^{-6}$ ; $m = 0.4942$ , $V_i = 12.86$ V
	Kowalski	$1.031 \times 10^{-7}$	$A_1 = 0.5578 \times 10^{-2}$ (m·Pa) $^{d-1}$ V $^{-d}$ ; $d = 1.277$ , $B_1 = -0.05594$ /V

**Fig. 1(a).** Gas gain *vs.* voltage for straw-tube chambers with five different anode-wire diameters, filled with P-10 gas.

**Fig. 1(b).** Gas gain *vs.* voltage for straw-tube chambers with five different anode-wire diameters, filled with Ar/Ethane (50/50) gas.

**Fig. 2.** Model fits to the gas gain in P-10 gas.

**Fig. 3.** Model fits to the gas gain in Ar/Ethane (50/50) gas.

Kowalski's formula is

$$\frac{\ln G}{V/\ln(R_c/R_a)} = \frac{A_1}{d-1} \left( \frac{V}{PR_a \ln(R_c/R_a)} \right)^{d-1} + B_1, \quad (3)$$

where  $A_1$ ,  $B_1$ , and  $d$  are constants of the gas.

The data points and fitted lines are shown in Fig. 2 and Fig. 3 for P-10 and Ar/Ethane, respectively. The variance used in the fitting for all of three formula is defined in the same way as

$$\text{Variance} = \sum_{i=1}^n \left( \frac{\ln(G_{\text{data}})_i}{V_i/\ln(R_c/R_{a,i})} - \frac{\ln(G_{\text{fit}})_i}{V_i/\ln(R_c/R_{a,i})} \right)^2 / n, \quad (4)$$

so we can directly compare their goodness of fit. The results are summarized in Table 1.

Only slight differences exist among the fits using the three models, so any could be used for the range of conditions we are studying.

## 2. Temperature dependence of the gas gain

The heat dissipation due to the electron/ion currents in a straw tube that comes within 10 cm of the beams at  $10^{32}$  luminosity at SSC is 1/3 mWatt.<sup>10</sup> This will heat up the gas and consequently the gas gain will be changed. In order to keep the gas gain within a desired range, the gas flow rate must be adequate to cool the heat load. But a large flow rate is difficult to accommodate in a compact straw-tube design, so it is important to know how strong is the temperature dependence of the gas gain.

### A. Experimental results

Because of an apparent lack of relevant data in the literature, we have placed the test chamber in an oven to make direct measurements of the temperature dependence. We are able to maintain a constant temperature inside of the oven to  $\pm 0.5^\circ\text{C}$ , as monitored by a thermocouple and microvoltmeter. The gas flow rate was reduced to a very low level to insure that the gas temperature inside the chamber was that of the surrounding oven.

Fig. 4 shows the experimental results for the P-10 gas mixture and the 0.0204-mm anode-wire chamber. Those for Ar/Ethane with 0.0204- and 0.127-mm anode-wire chambers are shown in Fig. 5. From these figures we draw the following qualitative conclusions:

1. The gas gain increases with temperature.
2. Different gas mixtures shows different temperature dependences; Ar/Ethane (50/50) is about 2.5 times as sensitive to temperature changes as P-10.
3. The temperature dependence of a 5-mil-diameter anode wire is about twice that of a 0.8-mil one;

**Fig. 4.** Temperature dependence of the gas gain in P-10 gas with an 0.8-mil-diameter anode wire.

**Fig. 5.** Temperature dependence of the gas gain in Ar/Ethane (50/50) with 0.8-mil and 5-mil-diameter anode wires.

**Fig. 6.** The ratio of relative gain change ( $dG/G$ ) to the relative temperature change ( $dT/T$ ) as a function of the gas gain in P-10 and Ar/Ethane (50/50) for 0.8-mil and 5-mil diameter anode wires.

4. The temperature dependence is stronger at larger gas gain.
5. A characteristic value of  $(dG/G)/(dT/T)$  is 5, as for Ar/Ethane (50/50) with an 0.8-mil-diameter anode wire and a gas gain of  $10^4$ . But see Fig. 6 for variations with gas type, gain, and anode-wire diameter.

## B. Model interpretation

Among the early works on gas amplification the well-known model proposed by Rose and Korff<sup>1</sup> has been cited by many authors. But this model is inadequate to reproduce the temperature dependence observed by us. The gas-gain formula derived from their model can be written as

$$\ln G = 2\sqrt{\frac{KNR_aV}{\ln(R_c/R_a)}} \left( \sqrt{\frac{V}{V_t}} - 1 \right), \quad (5)$$

where  $N$  denotes the gas density,  $V_t$  is the threshold voltage at which amplification starts to take place, and  $K$  is a constant.

The basic assumption of Rose and Korff was that

$$\alpha(r) = \langle N\sigma(U) \rangle$$

where  $\alpha(r)$  denotes the Townsend coefficient (defined by  $dn/n = -\alpha(r)dr$  where  $n$  is the number of ionization electrons), and  $\sigma(U)$  is the ionization cross section as a function of the electron energy  $U$ . The dependence of  $\alpha$  on the electric field  $E$  is through the latter's effect on the spectrum of energies  $U$ .

Assuming the gas pressure of the counter remains constant while the temperature is changing, it follows that

$$\frac{dN}{N} = -\frac{dT}{T}. \quad (6)$$

The gas density decreases with increasing temperature; therefore  $\alpha$  decreases too, according to the model of Rose and Korff, and as a consequence the gas gain decreases. This contrasts with our observation that the gas gain increases with increasing temperature.

Aoyama's model is based on different assumptions. He expressed  $\alpha$  as  $1/\lambda_r$  – the number of mean free paths per unit length in the field direction – multiplied by the chance of a free path length longer than  $\lambda_I$  – the mean path length for an electron to travel in the field direction to ionize a gas molecule, *i.e.*,

$$\alpha = \frac{1}{\lambda_r} e^{-\lambda_I/\lambda_r}, \quad (7)$$

where  $\lambda_I = V_I/E$ , and  $V_I$  is the effective ionization potential.

We can write

$$\frac{1}{\lambda_r} \approx \frac{1}{\lambda} = N\sigma,$$

since the mean free path along the field direction is approximately the same as the overall mean free path. Then the Townsend coefficient  $\alpha$  is approximately given as

$$\alpha = N\sigma \exp(-N\sigma V_I/E). \quad (8)$$

It follows that

$$\frac{d\alpha}{dN} = \sigma(1 - \lambda_I/\lambda_r) \exp(-N\sigma V_I/E). \quad (9)$$

The sign of  $d\alpha/dN$  will depend on the ratio of  $\lambda_I$  to  $\lambda_r$ . On differentiating both sides of eq. (2) and taking eq. (6) into consideration we obtain

$$\frac{dG/G}{dT/T} = A(1 - m) \ln G \left( \frac{E_a}{N} \right)^{m-1} = A(1 - m) \ln G \cdot S_a^{m-1}, \quad (10)$$

where we have introduced  $S_a \equiv E_a/P$  as the ratio of the electric field strength at the anode wire to the gas pressure. Similarly from eq. (1) and eq. (3) we get the following predictions according to Diethorn and Kowalski, respectively:

Diethorn's prediction:

$$\frac{dG/G}{dT/T} = \frac{\ln 2}{\Delta V \cdot \ln(R_c/R_a)} V. \quad (11)$$

Kowalski's prediction:

$$\frac{dG/G}{dT/T} = \frac{A_1}{\ln(R_c/R_a)} (S_a^{d-1} \cdot V). \quad (12)$$

Fig. 7 shows the comparison between our experimental data and these model predictions. The general trends are rather well predicted, but none of the models is able to make perfect predictions. The numerical disparities are within a factor of 2, and the experimental data are always below the model predictions, in which the model parameters were fitted using data taken at a constant temperature.

In summary:

- The gas-gain formulae proposed by Diethorn, Aoyama, and by Kowalski are able to describe the general behaviour of temperature dependence, and the predicted values could be safely used as upper limits.
- The most favorable (*i.e.*, smallest) empirical values for  $(dG/G)/(dT/T)$  are about half of the predicted values.

### 3. Electrostatic instability of the straw-tube chamber

Our goal is to build a large straw-tube tracking system. The length of each straw tube will be up to 2 m. It will greatly simplify the construction process and reduce the inefficient zone of the straw tube chamber if an extra support in the middle of the anode wire can be avoided.

**Fig. 7.** Comparison of experimental data on the temperature dependence of the gas gain with several models whose parameter were determined at a fixed temperature.

Cylindrical wire chambers are prone to an electrostatic instability in which the anode wire is pulled toward the cathode if the fields are strong enough. A general formula for the critical high voltage of stable operation of a straw tube chamber has been derived:<sup>11</sup>

$$V < \sqrt{\frac{T}{2\pi\epsilon_0} \frac{\pi R_c}{L} \ln\left(\frac{R_c}{R_a}\right)}, \quad (13)$$

where  $T$  is the tension of anode wire (Newtons),  $L$  is the length of wire (m), and  $\epsilon_0 = 8.85 \times 10^{-12}$  F/m. We will generalize this below.

We have studied the accuracy of eq. (13) with a 2-m-long tube, as sketched in Fig. 8. A 6.35-mm inner-diameter, 2-m-long stainless steel tube was fixed on a vertical unistrut channel by five adjustable rod-end bearings. By carefully adjusting the positions of these bearings we were able to secure the straightness of the tube to high accuracy. In the middle of the tube four 2-mm-diameter holes were drilled, equally spaced in  $90^\circ$  intervals. A green laser beam and a microscope eyepiece were employed to project the image of the hole and anode wire onto a screen as shown on the left of Fig. 8. The image of a 2-mm hole set the scale that was used to estimate the deviation of anode wire from its central location. The image of the hole and anode wire on the screen is sketched in Fig. 9. Actually the image of anode wire is a diffraction pattern, so it appears much wider than its geometrical image.

The results of these measurements are summarized in Tables 2-4. For each condition in Tables 3 and 4, a scan was made of the anode-wire displacement as a function of voltage. One such scan is given in Table 2. From each point in the scan we calculate the voltage-off displacement, labelled  $D_{\text{tube}}$ , of the wire using eq. (17) derived below. The several values of  $D_{\text{tube}}$  so deduced are nearly identical, which we take as verifying eq. (17).

Whenever the displacement of the anode wire reaches about 0.5 mm in our setup, an instability sets in. We label as  $V_{\text{max}}$  the voltage at which this occurs. For comparison, the voltage at which the displacement would be infinite according to eq. (17) is called  $V_0$ .

Observation shows that as the voltage is raised the anode wire experiences small but stable displacements, which go over into a large vibration at higher voltage. For practical purposes that latter conditions are unstable, and their onset defines the maximum operating voltage of the chamber.

The instability is aggravated if the anode wire is not concentric with the cathode tube. Here we extend that model of the instability to include this effect.

The capacitance per unit length of the straw-tube chamber as two cylinders not necessarily concentric is<sup>12</sup>

$$C = 2\pi\epsilon_0 \left[ \cosh^{-1} \left( \frac{R_c^2 + R_a^2 - D^2}{2R_c R_a} \right) \right]^{-1}.$$

The definitions of  $R_a$ ,  $R_c$ , and the anode-wire displacement  $D$  are illustrated in Fig. 10.

**Fig. 8.** Sketch of the setup to study the electrostatic instability of the anode wire. The left view shows the optical system to observe the deflection of the anode wire. The right view shows the mechanical alignment of the tube.

**Fig. 9.** Illustration of the effect of an anode-wire offset as observed on the viewing screen.

**Table 2.** A sample of wire instability measurements.

$T$ (gm)	$V$ (V)	Measured displacement of anode wire $D_{\text{wire}}$ (mm)	$V_0$ (V)	$(V_0/V)^2 - 1$	Calculated displacement of the tube $D_{\text{tube}}$ (mm)
20	0	0	1718		
	800	0.063		3.61	0.225
	900	0.13		2.64	0.336
	1000	0.16		1.95	0.310
	1100	0.22		1.44	0.320
	1200	0.32		1.05	0.333
	1250	0.38		0.89	0.339
	1300	0.51		0.75	0.379
	1350	unstable			
	40	0		0	2429
1000		0.063	4.9	0.306	
1200		0.13	3.1	0.393	
1400		0.19	2.01	0.383	
1600		0.25	1.31	0.331	
1700		0.32	1.04	0.331	
1750		0.38	0.93	0.353	
1850		unstable			

All data in Table 2 were taken with  $R_a = 0.0102$  mm.

When voltage  $V$  is applied between the cylinders the potential energy is

$$W = \frac{1}{2}CV^2.$$

The electric force  $F_E$  between anode wire and cathode can be derived by differentiating  $W$  with respect to  $D$ :

$$F_E = \frac{2\pi\epsilon_0 V^2}{R_c^2(\ln(R_c/R_a))^2} D = KD = K(D_{\text{tube}} + D_{\text{wire}}),$$

where  $D$  denotes the total deviation of the anode wire and tube from perfectly symmetrical geometry; in more detail,  $D_{\text{wire}}$  is the deviation of the wire from straightness, and  $D_{\text{tube}}$  is the displacement of the center of the tube from the ideal straight-line of the anode wire.

On the other hand, the restoring force  $F_T$  at the midpoint of the anode wire of length  $L$  is

$$F_T = T \left( \frac{\pi}{L} \right)^2 D_{\text{wire}},$$

**Table 3.** Electrostatic instability before fine adjustment of tube's straightness.

$R_a$ (mm)	Tension $T$ (gm)	Calculated Critical Voltage $V_0$ (V)	Measured Maximum Voltage $V_{\max}$ (V)	$V_{\max}/V_0$ (%)	Predicted Deviation of Tube from straight line $D_{\text{tube}}$ (mm)
0.0254	50	2283	1750	76.6	0.34
	100	3229	2450	75.8	0.29
	150	3954	*		0.29
	200	4567	*		0.28
0.0102	20	1718	1350	78.5	0.33
	40	2429	1850	76.1	0.36
	60	2976	*		0.34

\* Due to leakage currents inside the tube,  $V_{\max}$  could not be attained in these conditions.

**Table 4.** Instability during fine adjustment of tube's straightness.

Adjusted deviation of the tube from a straight line $D'_{\text{tube}}$ (mm)	Measured maximum voltage $V_{\max}$ (V)	$V_{\max}/V_0$ (%)	Predicted deviation of the tube from a straight line $D_{\text{tube}}$ (mm)
0 [case(1) in Fig.9]	1610	93.7	$5.7 \times 10^{-3}$
0.074 [case(2)]	1500	87.3	0.048
0.148 [case(2)]	1500	87.3	0.106
-0.074 [case(3)]	1505	87.6	-0.05
-0.148 [case(3)]	1505	87.6	-0.082

All data in Table 4 were taken with  $R_a = 0.0102$  mm, tension = 20 gm, for which the calculated critical voltage is  $V_0 = 1718$  V.

assuming the form of the deflection is

$$D(l) = D_{\text{wire}} \sin(\pi l/L).$$

For static equilibrium we have

$$F_T = F_E,$$

and hence

$$D_{\text{wire}} = D_{\text{tube}} \left[ \left( \frac{V_0}{V} \right)^2 - 1 \right]^{-1}, \quad (17)$$

**Fig. 10.** Geometry of an anode wire offset by distance  $D$  from the center of the cathode cylinder of a straw-tube chamber.

where

$$V_0 = \sqrt{\frac{T}{2\pi\epsilon}} \frac{\pi R_c}{L} \ln\left(\frac{R_c}{R_a}\right).$$

Given that a small lack of straightness,  $D_{\text{tube}}$ , is inevitable we see that the anode wire will be deflected from its initial position as the voltage rises.

Empirically, the wire becomes unstable once  $D_{\text{wire}}$  reaches about 0.5 mm in our setup, apparently independent of the value of  $D_{\text{tube}}$ . The physical mechanism underlying this remains to be clarified. It is possible that the instability is triggered by a discharge from the anode wire, which might be primarily sensitive to the electric field strength on the anode. If indeed there is a critical value,  $D_0$  for  $D_{\text{wire}}$  beyond which the instability sets in, we can write the stability condition as

$$V < V_0 \sqrt{\frac{D_0}{D_0 + D_{\text{tube}}}}. \quad (18)$$

(Remember that in (17) and (18),  $D_{\text{tube}}$  is the deviation of the tube from straightness, not its diameter.)

Tables 2-4 show the applicability of eq. (17). In Table 2,  $D_{\text{tube}}$  is inferred via eq. (17) by a series of observations of  $D_{\text{wire}}$  *vs.*  $V$ . A reasonably unique value of  $D_{\text{tube}}$  emerges from each scan, and it is the same value in scans in which the wire diameter was changed, but the tube was not. In Table 4 the wire diameter was constant, but the offset between the tube and wire, called  $D'_{\text{tube}}$ , was adjusted. Then the values of  $D_{\text{tube}}$  inferred from the voltage scan track the adjusted  $D'$  reasonably well.

Equation (17) also explains the experimental observations recently reported by Blockus *et al.*<sup>13</sup>

Conclusions:

**Fig. 11.** Calculated effect of a displacement  $D$  of the anode wire on the gas gain.

1.  $V_0$  is an upper-limit high voltage for operating a straw tube chamber. It appears possible to reach 90% of this upper-limit value.
2. For designing a large straw-tube system, 75% of  $V_0$  may be a more practical voltage for stable operation.
3. Any defect of roundness and straightness (including gravitational bending) of the straw tube itself will greatly affect the stability, as indicated by eq. (18).

#### 4. Effect of mechanical deviation on the gas gain

In a realistic straw-tube chamber there is always certain amount of mechanical deviation from the ideal symmetrical geometry. Therefore a gas-gain model, for example Diethorn's formula (1), should be modified as follows:

$$\ln G = \frac{V}{\cosh^{-1}(y)} \frac{\ln 2}{\Delta V} \left( \ln \frac{V}{PR_a \cosh^{-1}(y)} - \ln K \right),$$

where  $y = (R_a^2 + R_c^2 - D^2)/2R_aR_c$ , and  $D$  is the total displacement of the wire from the tube axis.

Fig. 11 shows the calculated curves of  $\ln G$  vs.  $D$  for three different sizes of anode wire. It is evident that the thicker wire is more sensitive to mechanical deviation. In the case of  $D = 0.5$  mm, the gas gain increases will be 5.6%, 8.3% and 11% for  $R_a = 0.01$  mm, 0.02 mm and 0.03 mm, respectively.

**Table 5.** Pros and cons of thick and thin wires.

Effect	Thick wire	Thin wire
Gravitational sagitta	same	same
Effect of mechanical deviation on gain	worse	better
Temperature dependence	worse	better
Electrostatic stability	better	worse

### 5. Choice of the wire size — thick or thin?

The choice of the wire size is a compromise among various considerations. We summarize some of them in Table 5.

Some supporting remarks:

Gravitational sagitta – For an anode wire of  $L$  (cm) in length,  $R_a$  (cm) in radius, under tension  $T$  (gm) and mounted horizontally, the sagitta is

$$s = 7.58L^2R_a^2/T,$$

while the maximum practical tension varies at  $T \propto R_a^2$  due to the breaking strength of the wire.

Mechanical deviation – see Fig. 10.

Temperature dependence – see Figs. 5, 6 and 7.

Electrostatic stability – Eq. (18) indicates that  $V_0 \propto \sqrt{T} \ln(R_C/R_A)$ , while  $T \propto R_a^2$ , so  $V_0 \propto R_a \ln(R_C/R_a)$ . On the other hand, the dependence of the gas gain on the wire radius is much slower than this, as shown by Diethorn’s formula (1).

### 6. An example

Since an Ar/Ethane (50/50) mixture has been used in the AMY vertex and inner-tracking chambers, and also was tested by MAC vertex-detector group, it is one of the best-understood gas mixtures for straw-tube chambers. We use the gas parameters of this mixture as found above to make a sample design of a straw-tube system.

We set the geometry of straw-tube chamber as

$$R_a = 0.00102 \text{ cm}, \quad R_c = 0.35 \text{ cm}, \quad L = 200 \text{ cm}.$$

In this example, the straw is mounted horizontally.

We use Aoyama's formula (2) for gas-gain calculations, with the parameters  $A = 0.1141 \times 10^{-6}$ ,  $m = 0.4942$ ,  $V_I = 12.86$  V; see Fig. 3.

If we want to operate our chamber at  $G \approx 2.5 \times 10^4$ , the high voltage should be set at  $V = 1550$  V.

From Fig. 7(c) we find  $(dG/G)/(dT/T) \approx 4.9$  under the present circumstances.

If we set tension  $T = 40$  gm, the gravitational sagitta will be  $75 \mu\text{m}$ , and the critical high voltage is  $V_0 = 2696$  V, yielding  $V/V_0 = 57.5\%$ .

According to eq. (17) the wire displacement  $D_w$  caused by electric field will be

$$D_w = \left[ \left( \frac{V_0}{V} \right)^2 - 1 \right]^{-1} \times 75 \mu\text{m} = 37 \mu\text{m}.$$

Therefore the total displacement of the anode wire from the tube center is

$$D_w = 75 + 37 = 112 \mu\text{m}.$$

This displacement will cause negligible variation of the gas gain, but will require a large correction to the position measurement.

Now we switch to a fat wire,  $R_a = 0.0254$  mm. If we still desire  $G = 2.5 \times 10^4$ , the high voltage should be set at  $V \approx 1960$  V.

A tension of 40 gm for  $R_a = 0.0102$ -mm wire scales up to  $T = 250$  gm at  $R_a = 0.0254$  mm. It follows that

$$V_0 = 5684 \text{ V},$$

$$V/V_0 = 34.4\%,$$

$$D_w = \left[ \left( \frac{V_0}{V} \right)^2 - 1 \right]^{-1} \times 75 \mu\text{m} = 10 \mu\text{m}.$$

Using Aoyama's formula (2) we can predict

$$\frac{dG/G}{dT/T} \approx 0.7 \times 9.5 = 6.6.$$

The spatial resolution attainable with Ar/Ethane (50/50) at 1 atm. is only about  $120 \mu\text{m}$  according to the measurements of MAC group<sup>14</sup> and AMY group<sup>8,15</sup>. In order to improve the spatial resolution high gas pressure could be used. If we run our chamber at 3 atm, the calculated results are summarized in Table 6. Note that a thin anode wire is not indicated at high pressure because the

**Table 6.** Summary of the design exercise.

$R_a$ (mm)	0.0102	0.0254	0.0102	0.0254
Gas pressure (atm)	1	1	3	3
Tension $T$ (gm)	40	250	40	250
Gain $G$ ( $\times 10^4$ )	2.5	2.5	2.5	2.5
$V$ (V)	1550	1960	2550	3450
$V_0$ (V)	2696	5684	2696	5684
$V/V_0$ (%)	58	34	95	60
$D_w^{\text{grav}}$ ( $\mu\text{m}$ )	75	75	75	75
$D_w^E$ ( $\mu\text{m}$ )	37	10	694	42
$D^{\text{Total}}$ ( $\mu\text{m}$ )	112	85	769	117
$(dG/G)/(dT/T)$	4.9	6.6	6.8	9.2

higher voltage required there renders the tube susceptible to the electrostatic instability.

## 7. Conclusion

1. The gas-gain models of Diethorn, Aoyama, and of Kowalski fit our experimental data (at a fixed temperature) rather well.

2. Experimental measurements have been made of the temperature dependence of the gas gain. The gas-gain formulae indicate the general behaviour of this dependence, but there is a substantial numerical disparity between data and the models, and the model values should be used only as an upper-limit estimate of temperature effects.

3. The critical voltage  $V_0$  of eq. (17) is a theoretical upper-limit value for stable operation of a straw-tube chamber: 90% of this value could be reached, but for a large straw-tube system, operation at 75% of  $V_0$  may be a more realistic number.

## References

1. M.E. Rose and S.A. Korff, *An Investigation of the Properties of Proportional Counters*, Phys. Rev. **59** (1941) 850.
2. W. Diethorn, US Atomic Energy Commission Report, NYO-6628 (1956).
3. A. Williams and R.I. Sara, Int. J. Appl. Radia. Isotopes **13** (1962) 229.
4. A. Zastawny, *Gas Amplification in a Proportional Counter with Carbon Dioxide*, J. Sci. Instr. **43** (1966) 179.
5. M.W. Charles, *Gas Gain Measurements in Proportional Counters*, J. Phys. **E5** (1972) 95.
6. T. Aoyama, *Generalized Gas Gain Formula for Proportional Counters*, N.I.M. **A234** (1985) 125.
7. T.Z. Kowalski, *Generalized parametrization of the Gas Gain in Proportional Counters*, N.I.M. **A243** (1986) 501.
8. M. Frautschi *et al.*, *The AMY Inner Tracking Chamber*, Ohio State U. preprint (Oct. 1989), submitted to N.I.M.
9. H. Frank, *Radiation Dosimetry*, (1966); Vol. I, Chap. 7.
10. C. Lu *et al.*, *Proposal to the SSC Laboratory for Research and Development of a Straw-Tube Tracking Subsystem*, Princeton U., DOE/ER/3072-56 (Sept. 39, 1989).
11. J. Carr and H. Kagan, *Wire stability studies for an SSC central drift tracker*, Proceedings of the 1986 Summer Study on the Physics of the SSC June 1986, p. 396.
12. W. Smythe, *Static and Dynamic Electricity* (McGraw-Hill, 1950).
13. D. Blockus *et al.*, *SSC Detector Subsystem Proposal, Central and Forward Tracking with Wire Chambers* (Oct. 1989), Fig. 2.9.
14. W.W. Ash *et al.*, *Design, Construction, Prototype Tests and Performance of a Vertex Chamber for the MAC Detector*, N.I.M. **A261** (1987) 399.
15. S.K. Kim, Private communication.